Unavoidable trees in tournaments

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An oriented tree $T$ on $n$ vertices is unavoidable if every tournament on $n$ vertices contains a copy of $T$. We obtained a sufficient condition for $T$ to be unavoidable, and use this to prove that almost all labeled oriented trees are unavoidable, verifying a conjecture of Bender and Wormald. We additionally proved that every tournament on $n+o(n)$ vertices contains a copy of every oriented tree $T$ on $n$ vertices with polylogarithmic maximum degree, improving a result of Kühn, Mycroft and Osthus. This is joint work with Richard Mycroft.